

Torsional Vibration Dependence on Transport Properties of DNA Molecules

Efta Yudiarsah
Universitas Indonesia
Depok, Indonesia

Regional School on Physics at the Nanoscale, Dec. 2009, Hanoi, Vietnam



Regional School on Physics at the Nanoscale, Dec. 2009, Hanoi, Vietnam

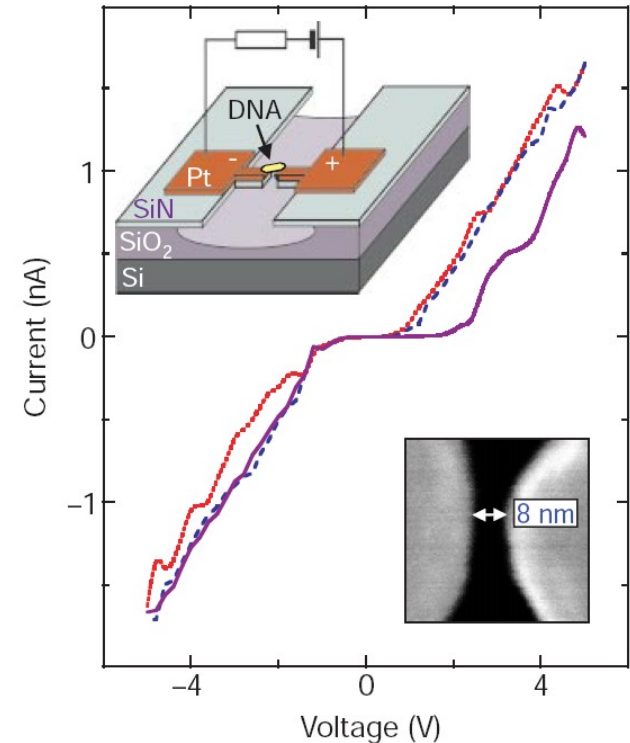


Outline

- **Motivation**
- **Torsional vibration dependence on transport properties of DNA molecules.**
- **Phonon effects on charge transport through a DNA base pair.**

Motivation

- **Molecular electronics**
- **Charge transfer in biology**
- **DNA can range from insulator to ohmic; Endres *et al.*, Rev. Mod. Phys. 76, 195 ('04)**
- **Conductivity depends on temperature; Yoo *et al.*, Phys. Rev. Lett. 87, 198102 ('01), Tran *et al.*, Phys. Rev. Lett. 85, 1564 ('00)**
- **Studying the effect of phonons**



30 bps poly(G)-poly(C)
large band-gap semiconductor

(Porath *et al.*, Nature 403, 635, (2000))

Torsional vibration dependence on transport properties of DNA molecules.

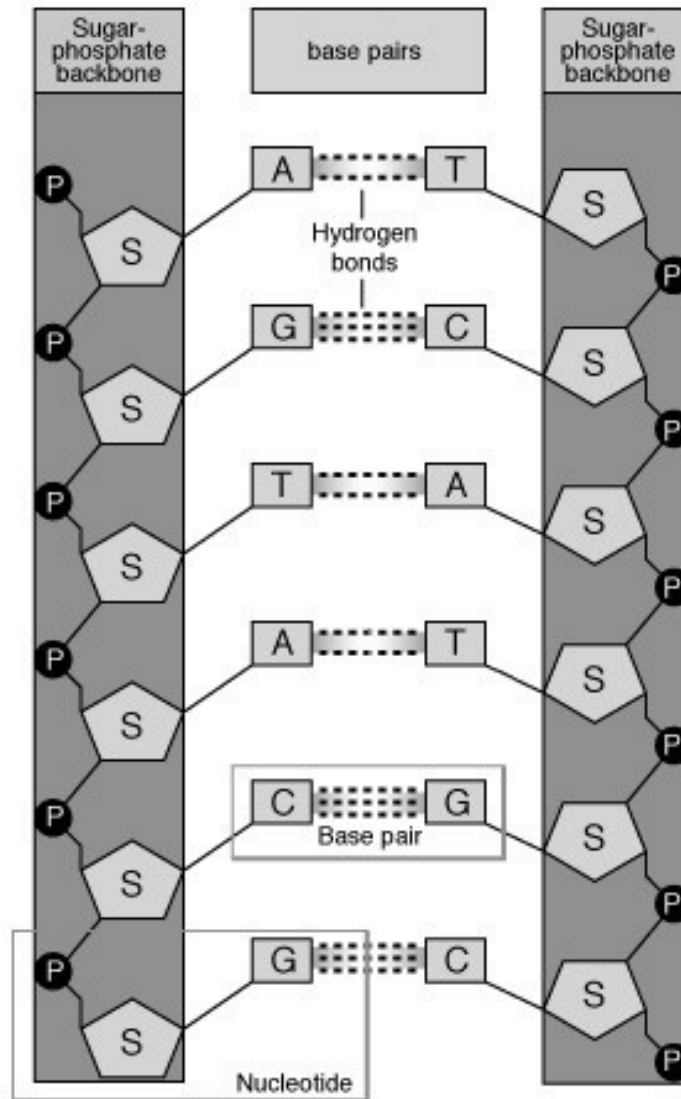
Daniel Kurnia, Efta Yudiarsah, and Rosari Saleh
Universitas Indonesia

The effect of temperature

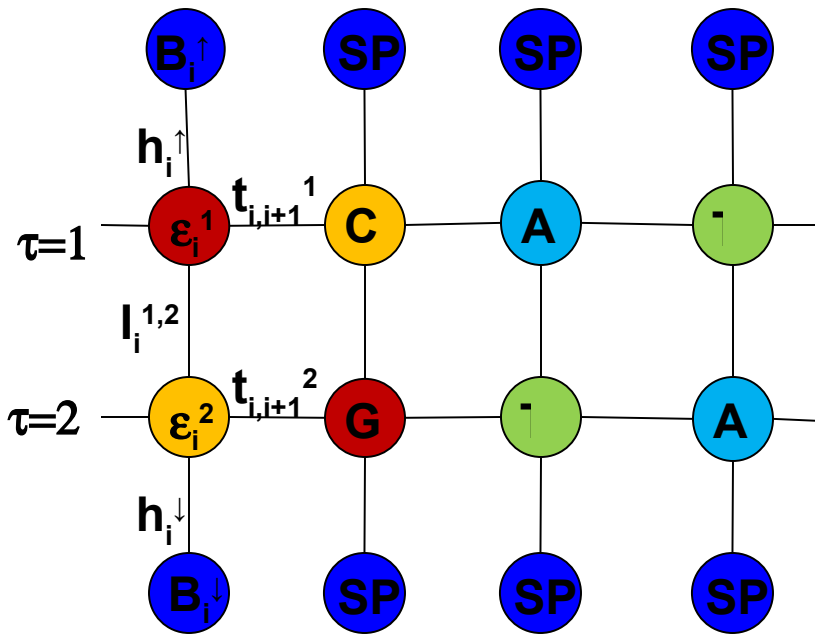
Ordered *sequence* → Poly(dG)-poly(dC)

Disordered *sequence* → Modified Poly(dG)-poly(dC): 50 GC base pairs replaced with 50 AT, TA, or CG base pairs

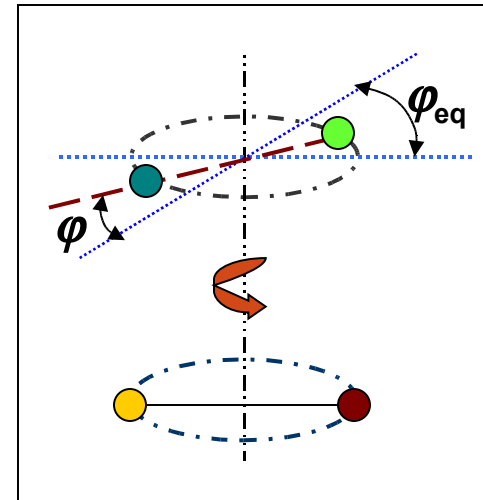
DNA Structure



2-Channel Model



100 base pairs long DNA sequence



Relative angle between two adjacent base pairs.

Angle follows a Gaussian distribution with zero average and standard deviation \sqrt{T} \rightarrow temperature
 \sqrt{f} \rightarrow $\sim \omega^2$

Hamiltonian

$$\begin{aligned}
 H = \sum_{i=1}^L & \left[\sum_{\tau=1}^2 \left\{ (\varepsilon_i^\tau + \phi_i^\tau) |i, \tau\rangle \langle i, \tau| + t_{i,i+1}^\tau \cos \Delta_{i,i+1} (|i, \tau\rangle \langle i+1, \tau| + \text{h.c.}) \right\} \right. \\
 & + \sum_{q=\downarrow}^{\uparrow} B_i^q |i, q\rangle \langle i, q| + \sum_{\{\tau, q\}=\{1, \downarrow\}}^{\{2, \uparrow\}} h_i^q (|i, \tau\rangle \langle i, q| + \text{h.c.}) \\
 & \left. + I_i (|i, 1\rangle \langle i, 2| + \text{h.c.}) \right]
 \end{aligned}$$

$$\phi_i^\tau = c_{i-1,i}^\tau (\cos \Delta_{i-1,i} - \cos \varphi_{eq}) + c_{i,i+1}^\tau (\cos \Delta_{i,i+1} - \cos \varphi_{eq})$$

$$\Delta_{i,i+1} = \varphi_{eq} - (\varphi_i - \varphi_{i+1})$$

$$\Delta_{i-1,i} = \varphi_{eq} - (\varphi_{i-1} - \varphi_i)$$

$$\begin{aligned}
 \varepsilon_G = 7.84 \text{ eV}, \quad \varepsilon_A = 8.22 \text{ eV}, \quad \varepsilon_C = 8.85 \text{ eV}, \\
 \varepsilon_T = 9.06 \text{ eV}, \quad \text{and} \quad \varepsilon_B = 9.36 \text{ eV}
 \end{aligned}$$

Transfer Matrix

Forward

$$\begin{pmatrix} \Psi_{i+1} \\ \Psi_i \end{pmatrix} = T_i \begin{pmatrix} \Psi_i \\ \Psi_{i-1} \end{pmatrix}$$

Backward

$$\begin{pmatrix} \Psi_{i-1} \\ \Psi_i \end{pmatrix} = T_i^b \begin{pmatrix} \Psi_i \\ \Psi_{i+1} \end{pmatrix}$$

$$T = T_1^b T_2^b \cdots T_{L-1}^b T_L^b T_L T_{L-1} \cdots T_2 T_1 \quad \text{Ndawana et al., Europhys. Lett. 68, 678 ('04)}$$

**Start with orthonormal matrix. Multiply with transfer matrix.
Orthonormalized every n steps. Keeping the coefficients (α).
Repeat K times**

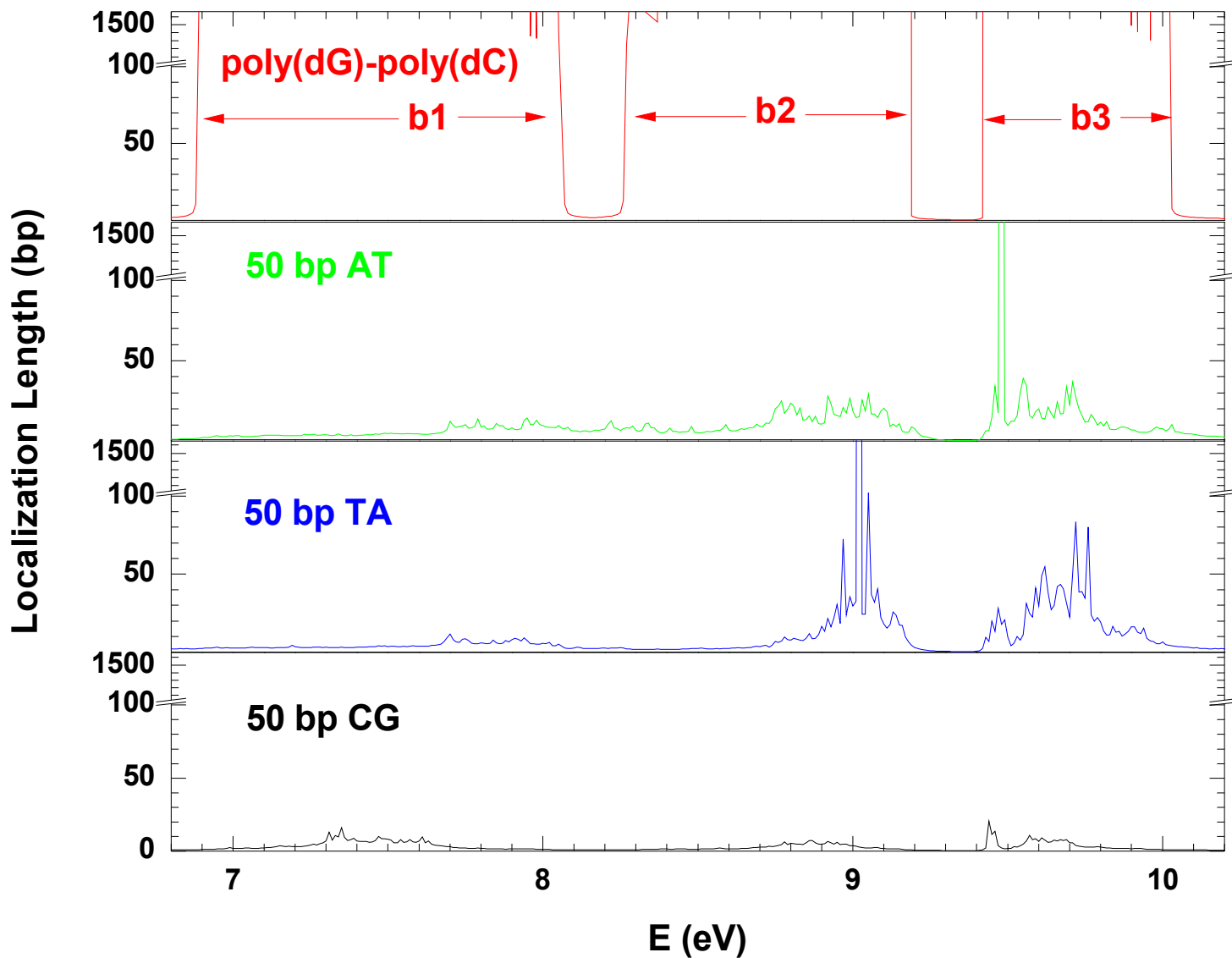
Lyapunov exponent

$$\gamma_{cl} = \frac{\ln \left(\prod_m \alpha_{cl}^m \right)}{2K(L-1)} \quad \longrightarrow \quad \text{Ortho-normalizing}$$

Ludlam, unpublished

Localization length = $1/\gamma_{\min}$

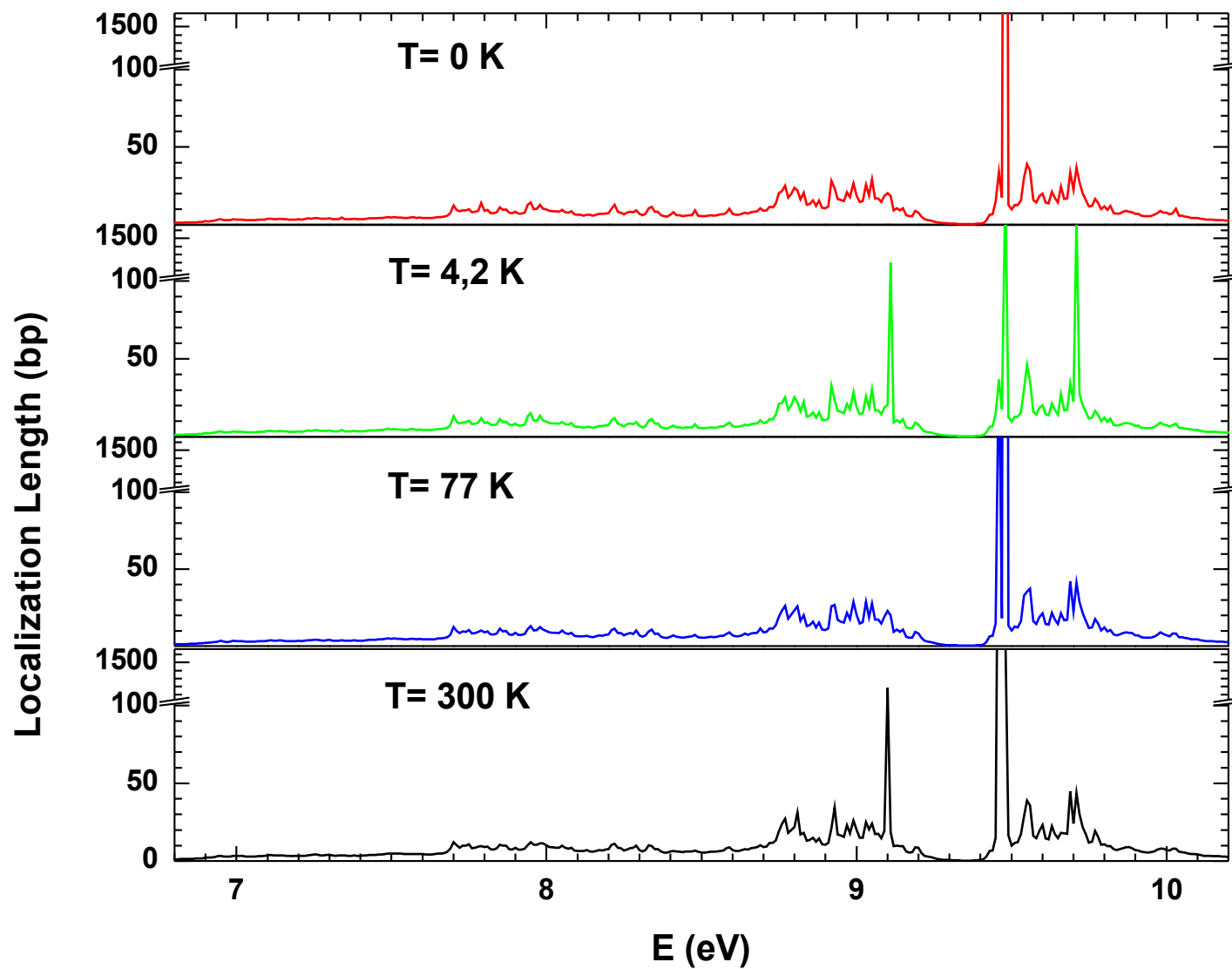
Disordered Sequence: Modified Poli(dG)-poli(dC)



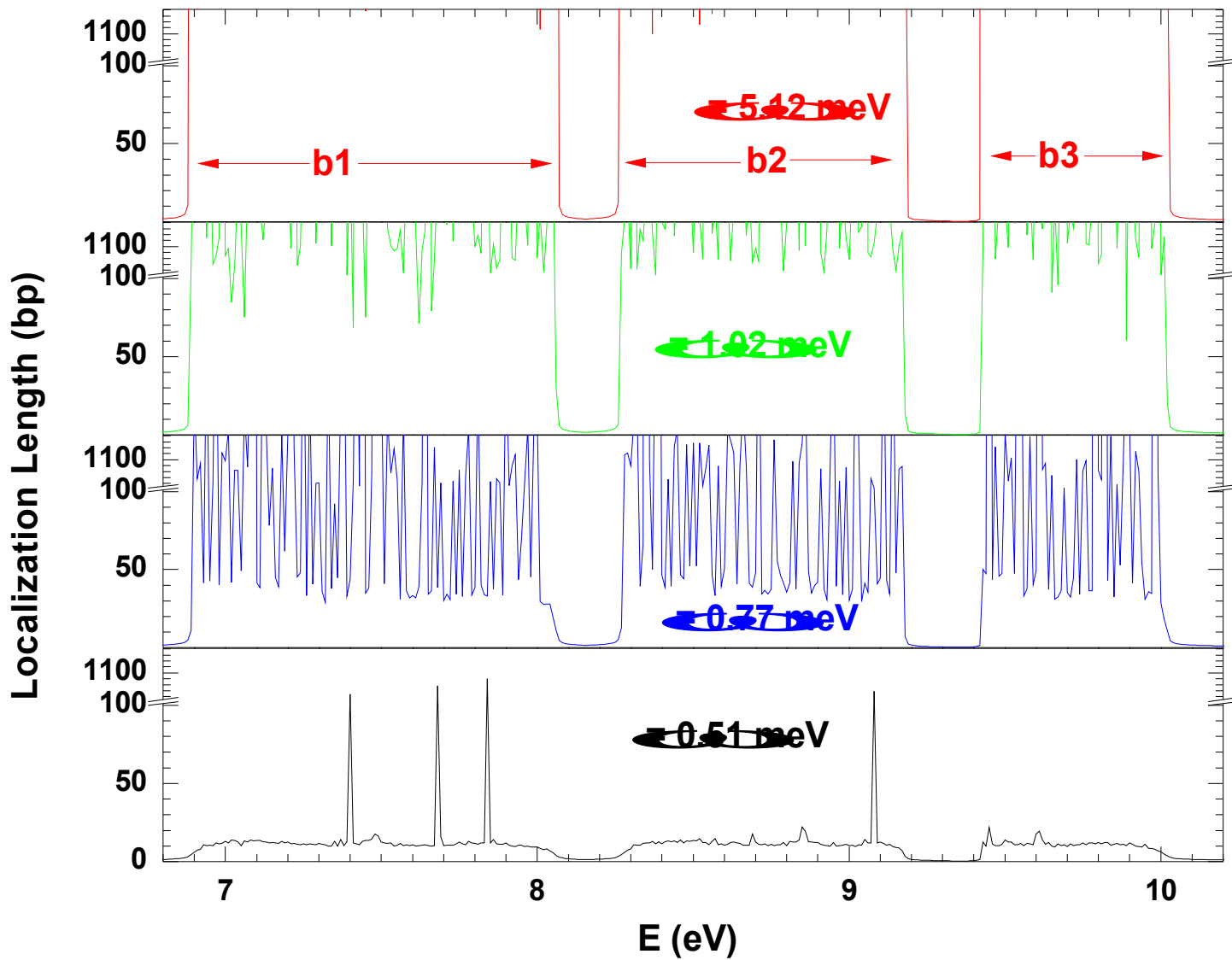
Agree with Roche, Phys. Rev. Lett. **91**, 108101 ('03) & Klotsa *et al.*, Biophys. J. **89**, 2187 ('05)

Temperature: Poli(dG)-poli(dC) modified with 50 bp AT

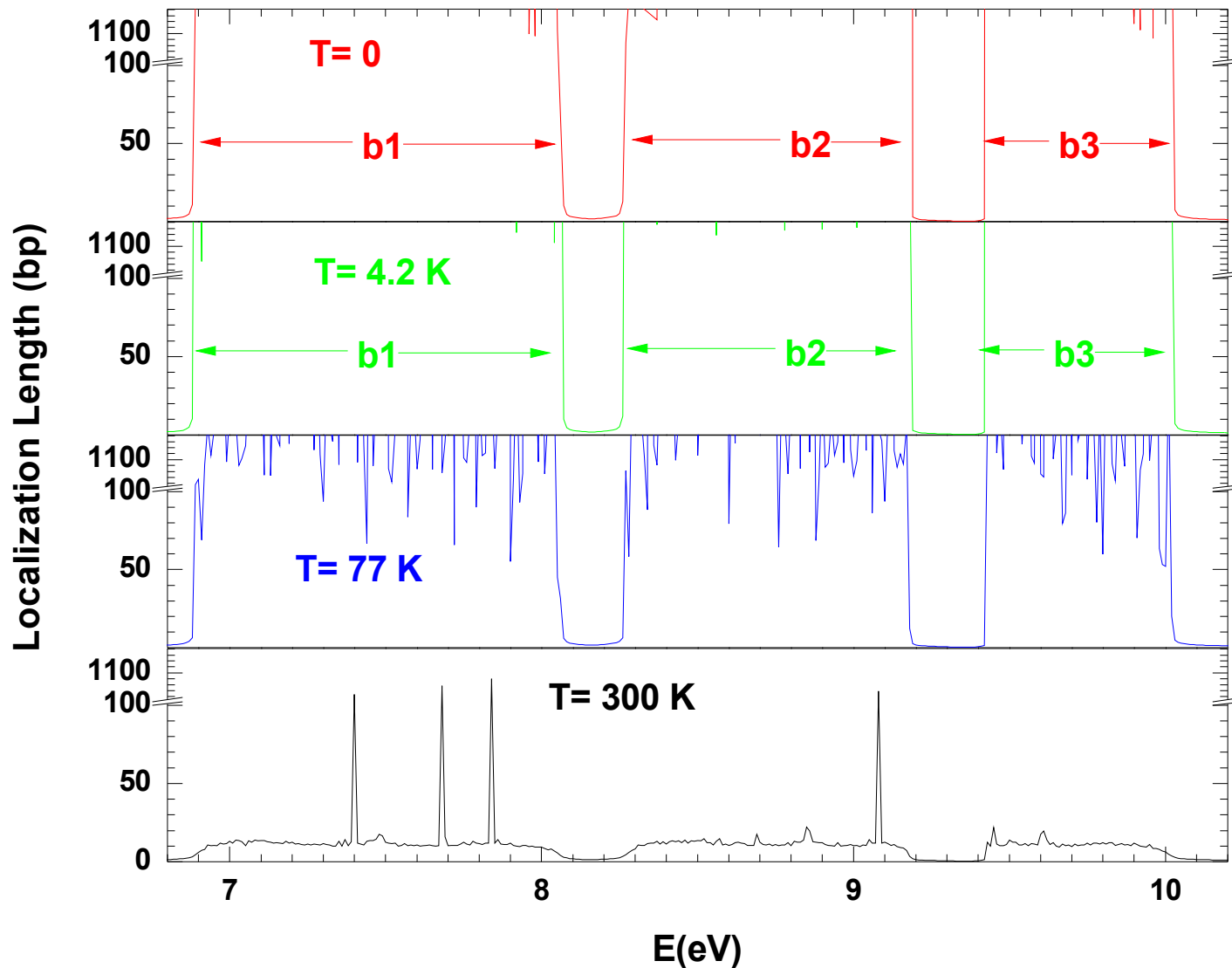
$\omega=5.12$ meV \rightarrow $\Delta\phi=9^\circ$ at 300 K



Frequency: Poli(dG)-poli(dC) pada T=300 K



Temperature: Poli(dG)-poli(dC) at $\omega = 0.51$ meV



Similar to Roche, Phys. Rev. Lett. **91**, 108101 ('03) and Ren *et al.*, Phys. Rev. B **72**, 035456 ('05)

Summary

- Disordered sequence \rightarrow localized state.
- Twisting frequency 5.12 meV \rightarrow little change to localization length with temperature.
- Twisting frekuensi 0.51 meV \rightarrow temperature changes the localization length.
- Lower twisting frequency \rightarrow lower localization length.

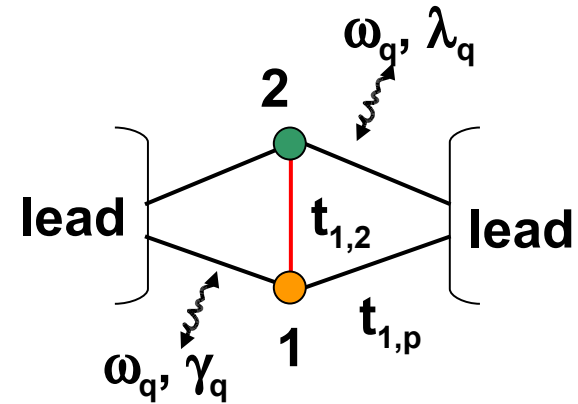
Phonon effects on charge transport through a DNA basepair

Efta Yudiarsah and Sergio E. Ulloa
Ohio University

Studying phonon and temperature effects on the transport through a molecule consists of two DNA bases.

Model

- ❖ 2 States model
- ❖ Hopping between the states
- ❖ Local electron-phonon interaction
- ❖ Non-local electron-phonon interaction



States energy

Hopping

Phonon

$$H_0 = \sum_j^2 \{ \varepsilon_j c_j^\dagger c_j \} + t_{1,2} (c_1^\dagger c_2 + c_2^\dagger c_1) + \sum_q \omega_q a_q^\dagger a_q + \sum_q \left\{ \sum_{j=1}^{j=2} \lambda_q (a_q + a_q^\dagger) c_j^\dagger c_j + \gamma_q (a_q + a_q^\dagger) [c_1^\dagger c_2 + c_2^\dagger c_1] \right\}$$

Local

Non-local

$\omega_0 = 1meV$ Locally interact with the electron

Polaron Shift $\Delta = g\omega_0; \quad g = (\lambda_0/\omega_0)^2$

$\omega_1 = 10meV$ Non-locally interact with the electron

Non-local electron-phonon interaction

$$\Sigma^q(\omega) = -\frac{1}{\beta} \sum_m D_q(i\omega_m) Y(\omega - i\omega_m)$$

Dressed electron Green's function

$$Y(\omega) = \begin{pmatrix} G_{22}(\omega) & G_{21}(\omega) \\ G_{12}(\omega) & G_{11}(\omega) \end{pmatrix}$$

Phonon Green's function

$$D_q(\omega)$$

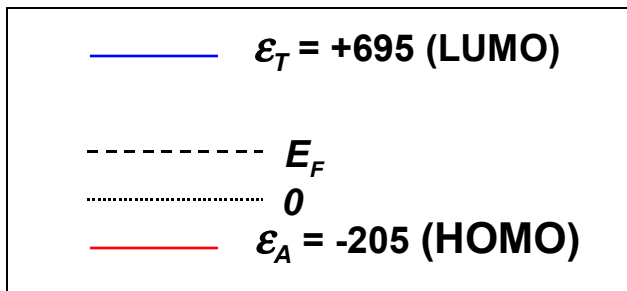
Symmetric Potential Drop at Contacts

Current: Meir and Wingreen, PRL'92

$$I = \frac{ie}{h} \int_{-\infty}^{+\infty} dE \operatorname{tr} \left\{ [\Gamma^L f_L(E) - \Gamma^R f_R(E)] [G^r(E) - G^r(E)] + [\Gamma^L - \Gamma^R] G^<(E) \right\}$$

Used parameter

On-site energy in meV; Roche, PRL'03

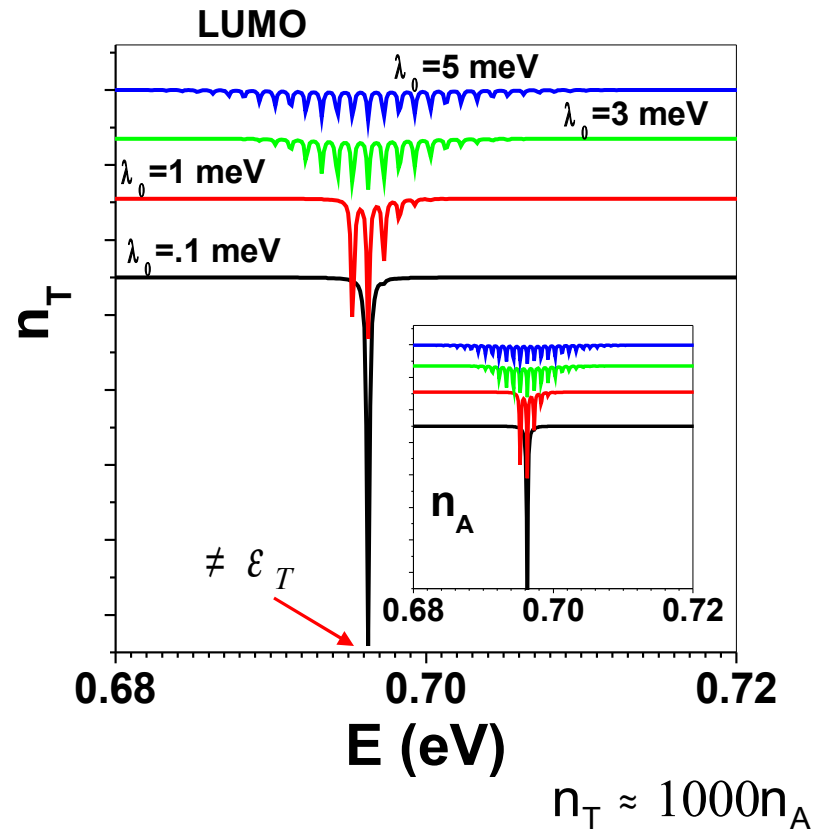
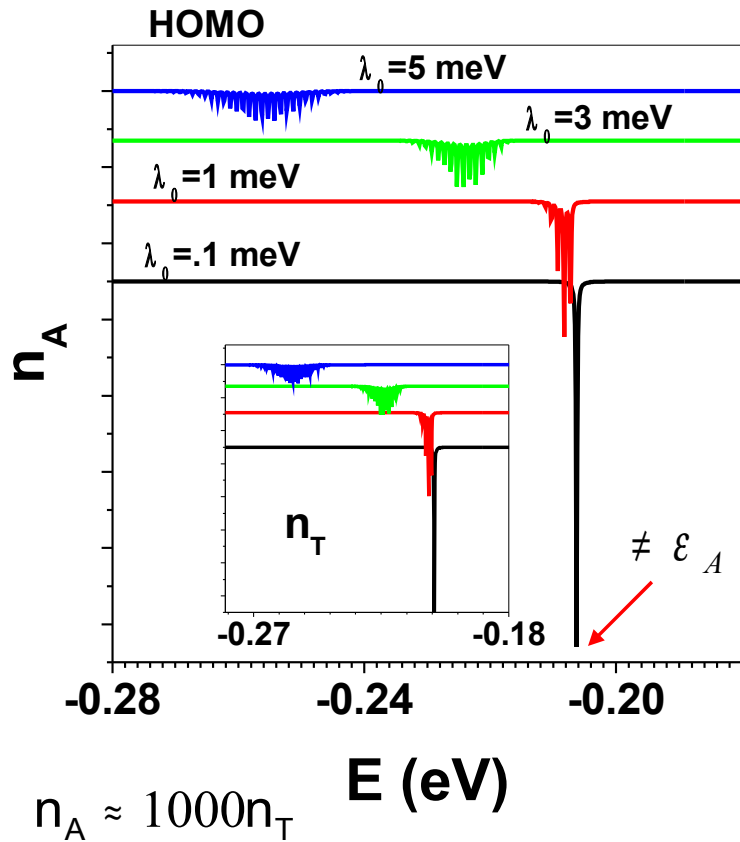


Coupling constant:

$t_{A,T} = 34$ meV; Voityuk *et al*

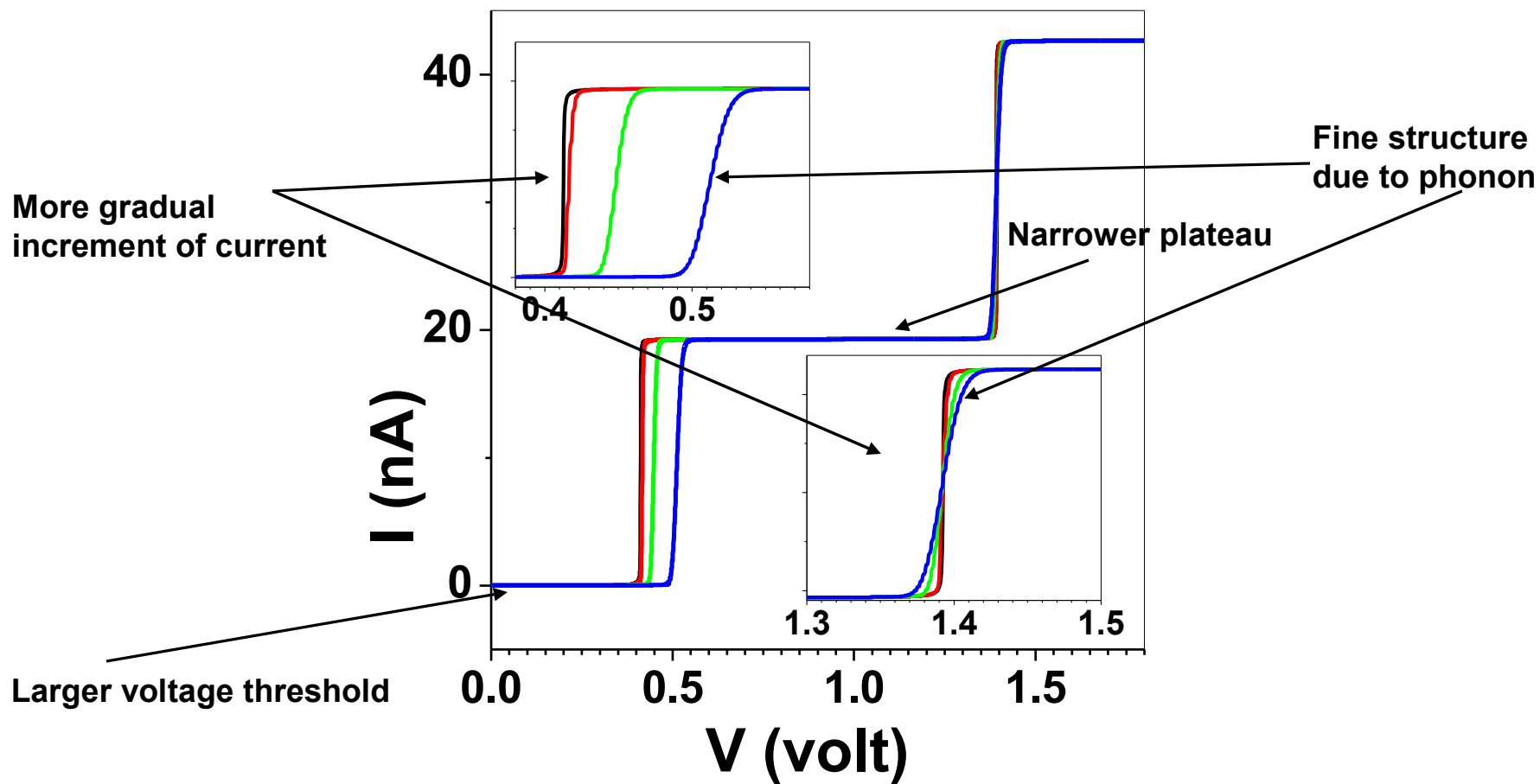
J Chem P '01

Polaronic Effect $T = 0K$ $\gamma_1 = .9meV$



- Shifted states \longleftarrow Polaron and tunneling
- Large g \longrightarrow larger polaron shift, more states, and lower density
- Envelope \longrightarrow Poisson distribution function at low T
- Maximum Peak at $2g\omega_0$ (HOMO) and constant (LUMO), for integer g

$$\gamma_1 = .9meV \quad E_F = 0eV$$



E_F close to HOMO \longrightarrow larger voltage threshold

E_F close to LUMO \longrightarrow smaller voltage threshold

Phonon Assisted Hopping $\lambda_0 = .9meV$ $T = 0meV$

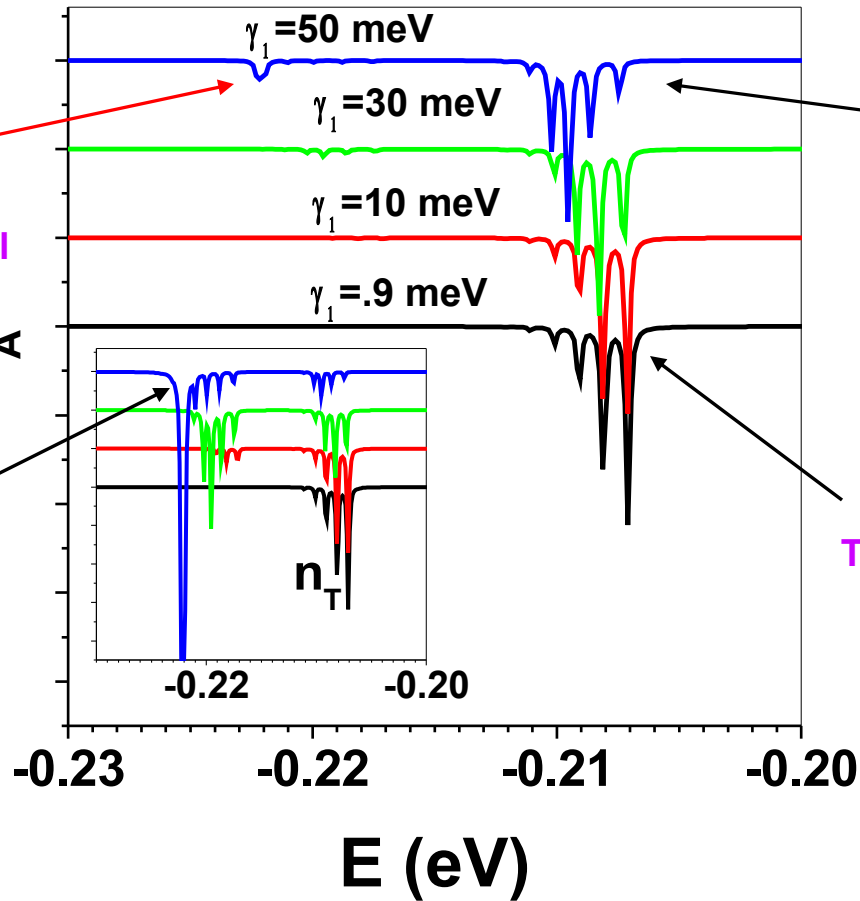
HOMO

$$\left\{ \frac{\gamma_1}{\omega_1} \right\}^2 > 1$$

Tunneling and off-diagonal self energy effect

Satellite group higher than main group

n_A



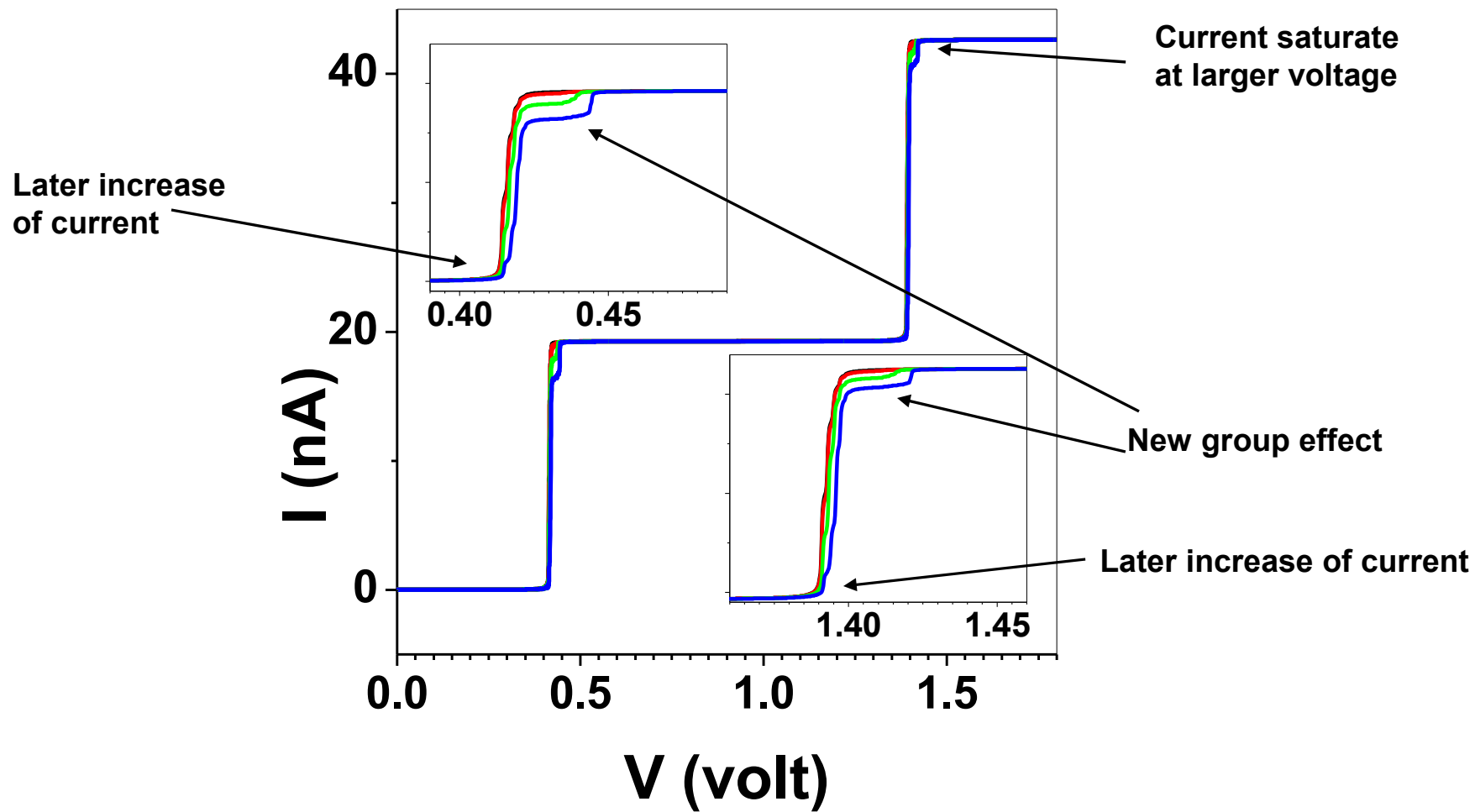
Satellite group lower than main group

$$\left\{ \frac{\gamma_1}{\omega_1} \right\}^2 < 1$$

Tunneling and off-diagonal self energy are small

Local and non-local interaction effect on shifting and the magnitude $\gamma^2 e^{-2g} \frac{g^{l+m}}{l!m!}$

Similar trends around LUMO state, but the shift to higher energy

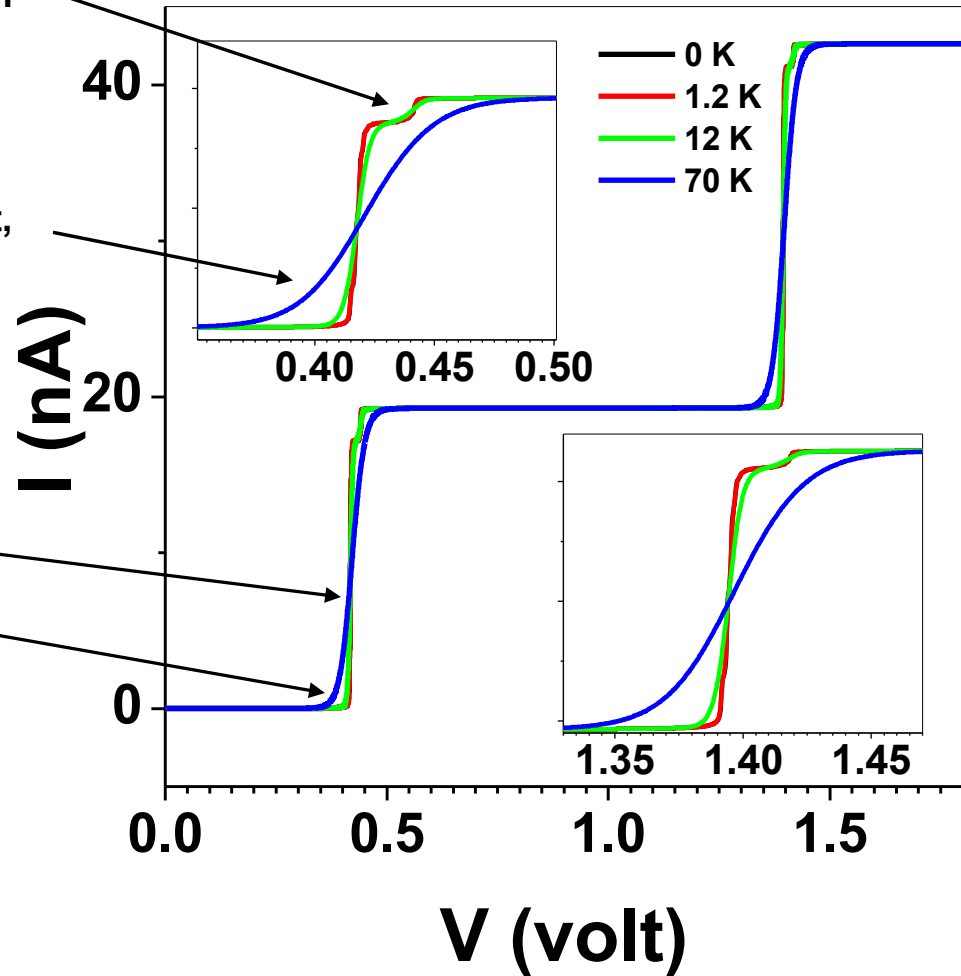


Temperature effects $\lambda_0 = .9\text{meV}$ $\gamma_1 = 40\text{meV}$

Separation of the transmission channels caused by local and non-local phonons

All fine structure is smeared out, Thermal energy $> \omega_0$

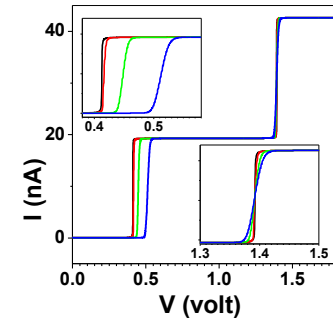
More States
More gradual increment of current
Smaller threshold



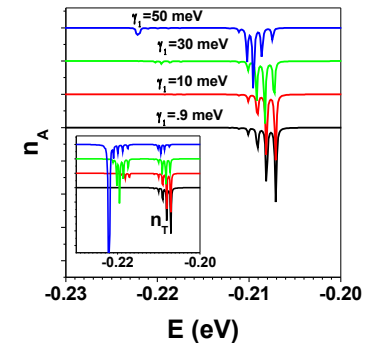
For small γ_1 a weaker effect is observed

Summary

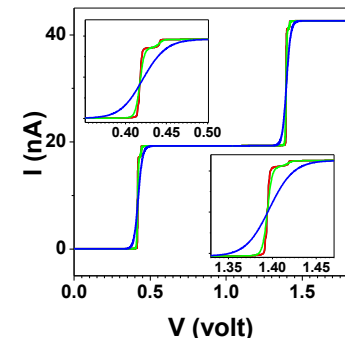
- Local interaction creates states with smaller amplitude. Similar to the result of Gutierrez *et al* PRB '06 and Schmidt *et al* PRB '07.
- More states and gradual current increment at stronger coupling.



- Non-local interaction introduces new states and shifts the position of the initial states. Similar to result of Schmidt *et al* PRB '07.
- More important off-diagonal self energy and the effect of coupling at stronger interaction. Non-linear effect shows up.



- More states, lower voltage threshold, and more gradual current increment.



Thanks for your attention

Regional School on Physics at the Nanoscale, Dec. 2009, Hanoi, Vietnam